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# THEORETICAL AND EXPERIMENTAL STUDY OF THE SORPTION PRO-CESSES OF GASES ON Nay ZEOLITES

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#### SUMMARY

Elementary processes involved in the sorption of gaseous  $N_2$ , CO,  $CO_2$ ,  $H_2O$ ,  $CH_4$ ,  $C_3H_8$ , n- $C_4H_{10}$ , iso- $C_4H_{10}$ ,  $C_2H_4$  and  $C_6H_6$  molecules on the surface of zeolite NaY were studied. A theoretical approach based on the method of empirical potentials and experimental determinations of the sorption energies by thermal desorption spectroscopy were used. The calculated sorption energies were compared with isosteric heats of sorption determined by gas chromatography. The nature of the interaction forces can be clearly seen from the profile of the individual energy components during sorption.

## INTRODUCTION

Zeolites (molecular sieves) are hetero-ionic adsorption materials widely used in gas chromatography (GC). From the theoretical point of view it is necessary to study the nature of the elementary sorption processes, to determine the stablest positions of sorbed molecules on the surface and to obtain the energy profile along the sorption path. These values can be used to acquire a deeper understanding of the sorption and separation processes.

Theoretical studies of the sorption processes on zeolites are in their infancy. Bezus and co-workers have calculated the interaction energies between NaX zeolites and molecules of rare gases<sup>1</sup>, some polar molecules<sup>2</sup> and selected alkanes<sup>3</sup>. There have also been attempts to use quantum chemical methods for such approaches<sup>4</sup>.

In this work we studied the sorption processes of  $N_2$ , CO, CO<sub>2</sub>, H<sub>2</sub>O, CH<sub>4</sub>, C<sub>3</sub>H<sub>8</sub>, *n*-C<sub>4</sub>H<sub>10</sub>, iso-C<sub>4</sub>H<sub>10</sub>, C<sub>2</sub>H<sub>4</sub> and C<sub>6</sub>H<sub>6</sub> with the surface of NaY zeolites by the method of empirical potentials. The theoretical results are compared with the sorption energies determined by thermal desorption spectroscopy and with isosteric heats of sorption determined by GC.

## THEORETICAL

The total energy of interaction (sorption energy) can be approximately expressed as a sum of individual contributions of dispersion, repulsion, coulombic (electrostatic) and inductive forces:

$$E = E_{\rm D} + E_{\rm R} + E_{\rm C} + E_{\rm I} \tag{1}$$

The dispersion term is expressed as<sup>5</sup>

$$E_{\rm D} = -\sum_{i} \sum_{j} C_{ij} r_{ij}^{-6}$$
(2)

where  $C_{ij}$  is the Kirkwood-Müller constant of dispersion attraction and  $r_{ij}$  is the distance between an atom of the sorbent *i* and an atom of a gas molecule *j*.

The repulsion term is<sup>5</sup>

$$E_{\rm R} = \sum_{i} \sum_{j} B_{ij} r_{ij}^{-12}$$
(3)

The constant  $B_{ij}$  is determined by the condition of minimum non-bonded interaction.

The electrostatic part of the sorption energy,  $E_c$ , corresponds to interactions between charges distributed on the atoms of zeolites and the charge distribution of sorbed molecules. In this work, for polar molecules we have used the term

$$E_{\rm C} = \frac{1}{4\pi\varepsilon_0} \sum_{i} \sum_{j} \frac{q_i q_j}{r_{ij}} \tag{4}$$

where  $\varepsilon_0$  is the permittivity of a vacuum and  $q_i$  and  $q_j$  are charges of atoms representing the surface and the gas molecule, respectively.

If the sorbed gas molecule has a permanent quadrupole moment, the electrostatic part of the interaction can be expressed as

$$E_{\rm C} = \frac{1}{16\pi\epsilon_0} \sum_{i} \sum_{j} q_i \,\theta_j (3\,\cos^2\,\varphi \,-\,1) r_{ij}^{-3} \tag{5}$$

where the angle  $\varphi$  corresponds to orientation of the quadrupole  $\theta$  of a molecule versus a position vector  $r_{ij}$ .

The inductive part of interaction energy is expressed as

$$E_{1} = \sum_{j} \frac{\alpha_{j}}{2} \cdot \varepsilon_{j}^{2}(r)$$
(6)

where  $\alpha_j$  is the polirizability of atom *j* of the gas molecule and  $\varepsilon_j(r)$  is the intensity of the electrostatic field which creates charges on the atoms in the zeolite. All constants used in eqns. 2-6 are taken from ref. 6.

## SORPTION OF GASES ON ZEOLITES

#### EXPERIMENTAL

Experimental values of the sorption energy  $(E_{tds})$  were determined by thermal desorption spectroscopy<sup>7</sup>. NaY molecular sieves were placed in a pumped vacuum system and successively heated from the temperature of liquid nitrogen to room temperature. From the desorption spectrum, *i.e.*, the dependence of pressure changes on the temperature of the surface, activation energies of desorption were evaluated. In cases of physical adsorption the activation energy of sorption is equal to the sorption energy.

Isosteric heats of sorption,  $Q_{is}$ , of some gases determined by GC were taken from the literature<sup>8</sup>.

### **RESULTS AND DISCUSSION**

The surface of NaY zeolites is represented by ten cubo-octahedrons surrounding a large cavity of zeolite (Fig. 1). Each cubo-octahedron contains 48 atoms of oxygen with negative charges and 14 atoms of sodium with positive charges. A total of 620 atoms of oxygen and sodium were considered. The effect of Al and Si is included in the effective charge on O and Na.

To calculate interaction (sorption) energies, two computer programs were used. Program I finds the stablest position of a gas molecule in the large cavity of the zeolite. This position corresponds to the minimum of an interaction energy curve.



Fig. 1. Model of NaY zeolite.

Molecule	Experimental $(kJ mol^{-1})$		Calculated $(kJ mol^{-1})$	
	Q <sub>is</sub> (GC)	E <sub>tds</sub>	Program I	Program II
 N <sub>2</sub>		29.4	23.6	20.2
cõ	24.3	31.2	25.6	21.8
CO <sub>2</sub>		53.2	48.4	39.5
H₂Ō		87.4	83.2	81.2
CH₄	18.4		18.8	18.1
C <sub>3</sub> H <sub>8</sub>	34.1	36.4	33.9	30.3
$n-C_4H_{10}$		50.9	48.9	47.5
iso-C <sub>4</sub> H <sub>10</sub>		65.5	64.2	61.1
C₂H₄	45.7	43.6	40.6	38.5
C <sub>6</sub> H <sub>6</sub>		88.6	90.2	86.4

CALCULATED AND EXPERIMENTAL VALUES OF SORPTION ENERGIES

Program II calculates the energy of sorption along a three-fold symetry axis passing through a large cavity window towards the sorption centre  $S_{II}$ . The curve of the total interaction energy is the sum of the curves of the dispersion, repulsion, electrostatic and inductive energy components.

The calculated values of the sorption energies of individual gases evaluated by programs I and II are given in Table I, and are compared with experimental values. A qualitative agreement is obtained between the energies  $E_{tds}$  and those calculated by program I. The values obtained by program II are generally lower than those obtained by program I. Program I optimizes the position of a sorbed molecule in all



Fig. 2. Curves of the individual energy terms during adsorption of an N<sub>2</sub> molecule.

TABLE I



Fig. 3. Curves of the individual energy terms during adsorption of an H<sub>2</sub>O molecule.

the space of the large cavity of the zeolite, whereas the values obtained by program II correspond to minima near to sorption centre  $S_{II}$ . Although in most instances calculated optimal positions of sorbed molecules are close to the centre  $S_{II}$ , the difference between energies calculated by the two programs are small. Values of isosteric heats of sorption  $Q_{is}$ , determined by GC are not known for all the gases considered on the NaY zeolites. It should be stressed that a direct comparison with calculated values is possible if the value RT (2.4 kJ mol<sup>-1</sup> at 300 °K) is subtracted from  $Q_{is}$ .

The nature of the interaction forces acting in sorption and separation processes can be clearly seen from the calculated energy profile. For non-polar molecules (N<sub>2</sub>, CO<sub>2</sub>, alkanes, etc.) the sorption process is governed by the dispersion component of the interaction energy. Fig. 2 shows energy profiles of adsorption of N<sub>2</sub> on NaY zeolites. For slightly polar molecules the coulombic component contributes to total stabilization. For polar molecules such as H<sub>2</sub>O the coulombic component is dominant (Fig. 3). The induction component is important, especially for larger molecules such as C<sub>6</sub>H<sub>6</sub> (Fig. 4).

The theoretical values obtained by this approach can be used for the calculation of other thermodynamic quantities  $(H, S, \text{Henry's constant, etc.})^1$ . This method also enables the model of the surface of zeolites to be modified and necessary changes in the surface to be predicted in order to obtain desirable sorption and separation properties. We shall consider these problems in subsequent papers.



Fig. 4. Curves of the individual energy terms during adsorption of a  $C_6H_6$  molecule.

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## REFERENCES

- 1 A. G. Bezus and C. E. Dobrova, Kolloidn. Zh., 37 (1975) 1045.
- 2 A. G. Bezus, A. V. Kiselev and Fam Kuang Zy, Dokl. Akad. Nauk SSSR, 237 (1977) 126.
- 3 A. G. Bezus and M. Kočiřík, Adsorption of Hydrocarbons in Zeolites, Akademie Verlag, Berlin, 1979, p. 56.
- 4 J. Sauer, P. Hobza and R. Zahradník, J. Phys. Chem., in press.
- 5 M. Born and J. E. Mayer, Z. Phys., 75 (1932) 1.
- 6 J. Miertušová, Thesis, Comenius University, Bratislava, 1981.
- 7 G. Carter, Vacuum, 12 (1962) 245.
- 8 V. Patzelová, Chem. Zvesti, 29 (1975) 331.